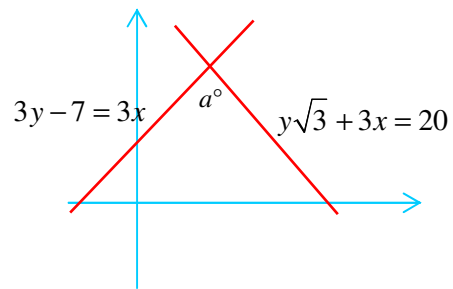


**Banker Short Question: No. 1**

- a) Find the equation of the line through  $(3, -2)$  parallel to the line  $2y = 3x + 5$
- b) Find the equation of the line through  $(-1, -3)$  perpendicular to the line  $3y - x + 7 = 0$
- c) Find the angle that the line  $5y + 2x + 3 = 0$  makes with the positive direction of the  $x$ -axis
- d) Find the angle marked  $a$  in the diagram, between the lines  $3y - 7 = 3x$  and  $y\sqrt{3} + 3x = 20$



[Scroll to next page to see solutions]

## Banker Short Question: No. 1

### Solution.

a) Arrange the line into normal form to extract the gradient.

$$y = \frac{3}{2}x + \frac{5}{2} \text{ hence gradient} = \frac{3}{2}$$

Line parallel has same gradient.

$$\text{So line is: } y - (-2) = \frac{3}{2}(x - 3)$$

Simplify:

$$y + 2 = \frac{3}{2}(x - 3) \rightarrow 2y + 4 = 3x - 9$$

$$\rightarrow 2y - 3x + 13 = 0$$

b) Arrange the line into normal form to extract the gradient.

$$3y = x - 7 \rightarrow y = \frac{1}{3}x - \frac{7}{3}$$

Hence gradient is  $\frac{1}{3}$

Gradient of perpendicular line:  $-3$

$$\text{(since } m_2 = -\frac{1}{m_1}\text{)}$$

$$\text{So line is: } y - (-3) = -3(x - (-1))$$

Simplify:

$$y + 3 = -3(x + 1)$$

$$y + 3 = -3x - 3$$

$$y + 3x + 6 = 0$$

c) Arrange to normal form:

$$5y = -2x - 3 \rightarrow y = -\frac{2}{5}x - \frac{3}{5}$$

hence gradient is:  $-\frac{2}{5}$

Using  $m = \tan \theta$

$$\tan \theta = -\frac{2}{5} \text{ acute } \theta = \tan^{-1}\left(\frac{2}{5}\right) = 21.8^\circ$$

since tan is negative then  $\theta$  must be obtuse.

$$\text{Hence } \theta = 180 - 21.8 = 158.2^\circ$$

[Scroll to next page to see solution for part (d)]

## Notes on solution

You must have the equation in normal form:

$$y = mx + c$$

before you can extract the gradient.

Parallel lines have the same gradient.

Use formula:

$$y - b = m(x - a)$$

Any simplified form will do unless form is specified.

Multiply to get rid of fractions.

You must have the equation in normal form:

$$y = mx + c$$

before you can extract the gradient.

Say what you are doing here.

Make reference to  $m_2 = -\frac{1}{m_1}$

Use formula:

$$y - b = m(x - a)$$

Any simplified form will do unless form is specified.

Multiply to get rid of fractions.

You must have the equation in normal form:

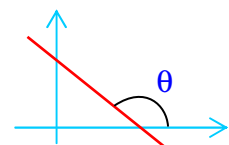
$$y = mx + c$$

before you can extract the gradient.

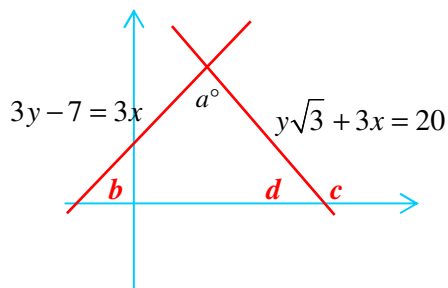
Use:  $m = \tan \theta$

Remember if  $m$  is negative, then  $\tan \theta$  is negative and so the angle is obtuse.

The angle is **ALWAYS** the anticlockwise angle between the line and the x-axis.



d)



Find gradient of  $3y - 7 = 3x$

Rearrange:  $3y = 3x + 7 \rightarrow y = x + \frac{7}{3}$

Hence gradient = 1

Using  $m = \tan \theta \rightarrow \tan \theta = 1$

So angle marked **b** on diagram =  $45^\circ$

Find gradient of  $y\sqrt{3} + 3x = 20$

Rearrange:  $y\sqrt{3} = -3x + 20$

$$y = -\frac{3}{\sqrt{3}}x + \frac{20}{\sqrt{3}}$$

So:  $y = -\sqrt{3}x + \frac{20}{\sqrt{3}}$

Hence gradient is:  $-\sqrt{3}$

Using  $m = \tan \theta \rightarrow \tan \theta = -\sqrt{3}$

So acute  $\theta = 60^\circ$ , but tangent is negative, so  $\theta$  is obtuse.

Hence  $\theta = 180 - 60 = 120^\circ$ ,

So angle marked **c** on diagram =  $120^\circ$

Furthermore, angle **d** on the diagram must be  $60^\circ$ .

So using the fact that angles in a triangle add up to  $180^\circ$ , then:

$$a = 180 - 45 - 60 = 75^\circ$$

You must have the equation in normal form:

$$y = mx + c$$

before you can extract the gradient.

Surds and gradients often indicate the table of exact values.

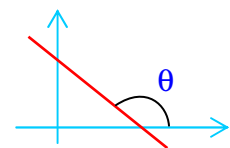
When you encounter surds the following note is always useful.

Note that:  $-\frac{3}{\sqrt{3}} = -\frac{\sqrt{3}\sqrt{3}}{\sqrt{3}} = -\sqrt{3}$

Use:  $m = \tan \theta$

Remember if  $m$  is negative, then  $\tan \theta$  is negative and so the angle is obtuse.

The angle is **ALWAYS** the anticlockwise angle between the line and the x-axis.



Angles in a triangle add up to 180

**Use the diagram to clarify your thoughts.**